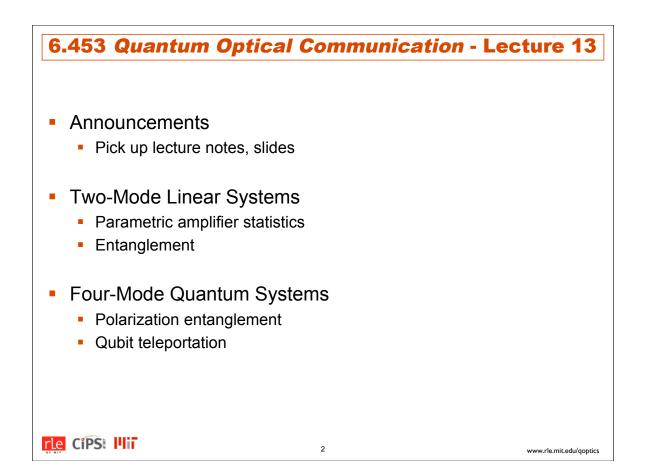
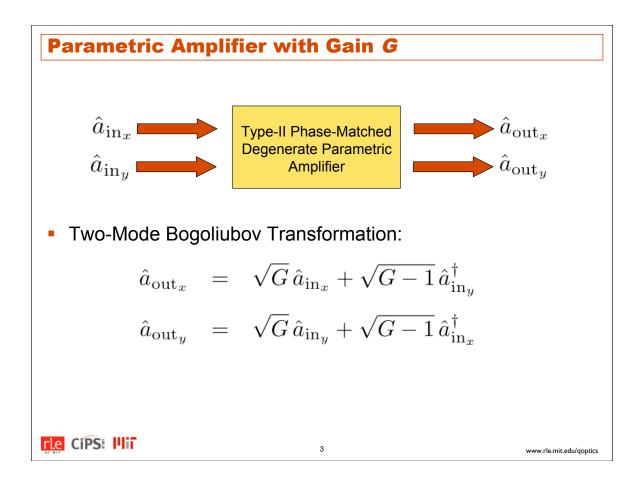
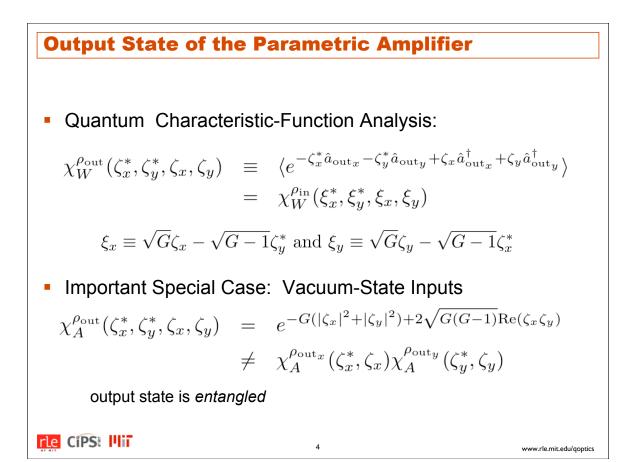
6.453 Quantum Optical Communication Spring 2009

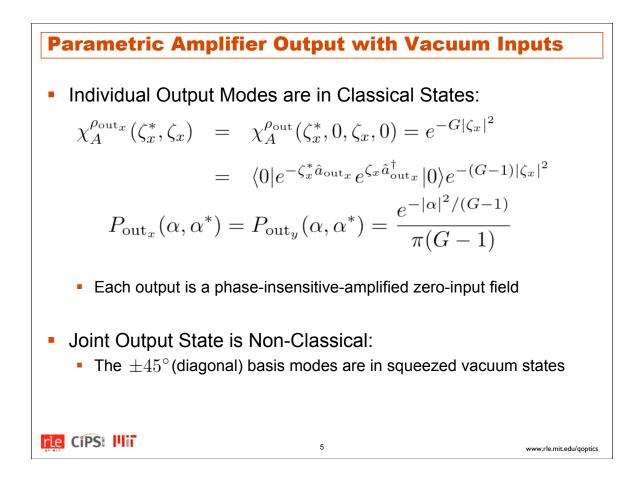
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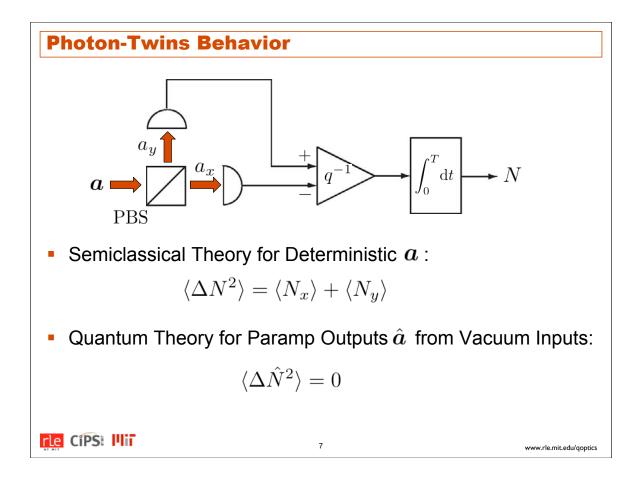
Parametric Amplifier Output with Vacuum Inputs

 • Squeezed-Vacuum Representation:

$$|\psi\rangle_{out} = |\psi\rangle_{out_{45}}|\psi\rangle_{out_{-45}}$$
 $= |0; \sqrt{G}, -\sqrt{G-1}\rangle_{45} |0; \sqrt{G}, \sqrt{G-1}\rangle_{-45}$

 • Photon-Twins Representation:

 $|\psi\rangle_{out} = \sum_{n=0}^{\infty} \sqrt{\frac{(G-1)^n}{G^{n+1}}} |n\rangle_x |n\rangle_y$



Reduced Density Operators for Paramp Outputs

• Measure Observable $\hat{O}_x = \sum_n o_n |o_n\rangle_x \, _x\langle o_n|$:

$$\Pr(\hat{O}_x = o_n \mid |\psi\rangle_{\text{out}}) = \operatorname{tr}[\hat{\rho}_{\text{out}}(|o_n\rangle_{x\,x}\langle o_n \mid \otimes \hat{I}_y)]$$
$$= \operatorname{tr}(\hat{\rho}_{\text{out}_x}|o_n\rangle_{x\,x}\langle o_n \mid)$$

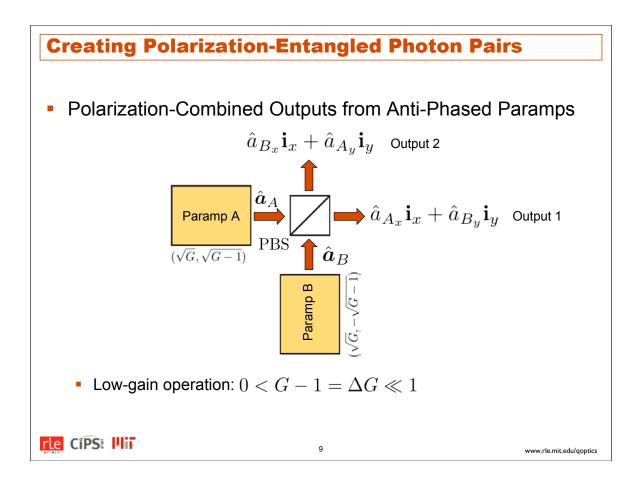
implies $\hat{\rho}_{\mathrm{out}_x} = \mathrm{tr}_y(\hat{\rho}_{\mathrm{out}})$

For the Parametric Amplifier with Vacuum-State Inputs

$$\hat{\rho}_{\text{out}_k} = \sum_{n=0}^{\infty} \frac{(G-1)^n}{G^{n+1}} |n\rangle_{k \ k} \langle n|, \quad \text{for } k = x, y$$

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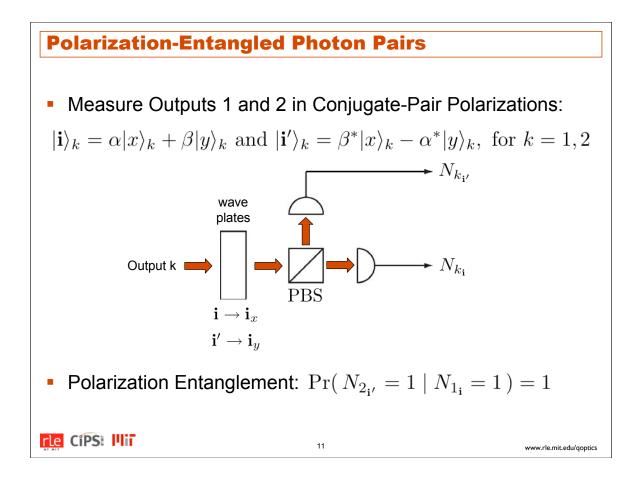


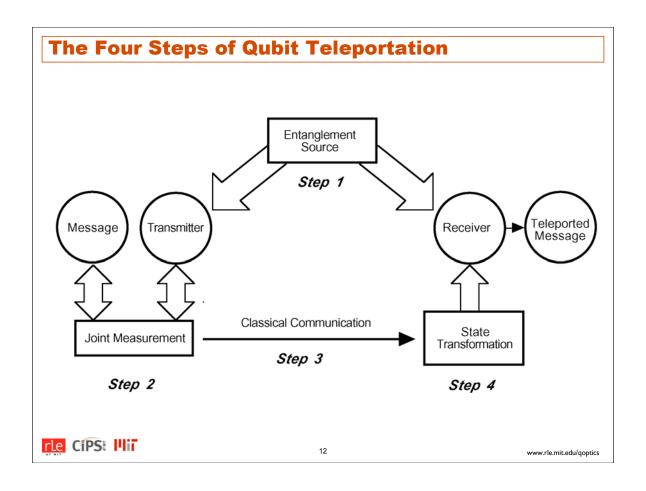
Creating Polarization-Entangled Photon Pairs
• Dual-Paramp Output State in Low-Gain Limit:

$$|\psi\rangle_{out} = |\psi\rangle_A \otimes |\psi\rangle_B$$

 $= \sum_{n=0}^{\infty} \sqrt{\frac{\Delta G^n}{G^{n+1}}} |n\rangle_{A_x} |n\rangle_{A_y} \otimes \sum_{m=0}^{\infty} (-1)^m \sqrt{\frac{\Delta G^m}{G^{m+1}}} |m\rangle_{B_x} |m\rangle_{B_y}$
 $\approx (|0\rangle_{A_x} |0\rangle_{B_y}) \otimes (|0\rangle_{B_x} |0\rangle_{A_y})$
 $+ \sqrt{\Delta G} [(|1\rangle_{A_x} |0\rangle_{B_y}) \otimes (|0\rangle_{B_x} |1\rangle_{A_y}) - (|0\rangle_{A_x} |1\rangle_{B_y}) \otimes (|1\rangle_{B_x} |0\rangle_{A_y})]$
• Entangled Bi-Photon State Realized by Post-Selection:
 $\frac{1}{\sqrt{2}} (|x\rangle_1 |y\rangle_2 - |y\rangle_1 |x\rangle_2)$

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Coming Attractions: Lecture 14 + Schedule Notes Lecture 14: Teleportation Polarization entanglement and qubit teleportation Quadrature entanglement and continuous-variable teleportation Schedule Notes: Term paper proposals are due Thursday, November 6 Mid-term exam Thursday, November 6